#### Chapter 6

#### Data Directed Importance Sampling for Climate Model Parameter Uncertainty Estimation

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## Abstract

Assessments of uncertainty in climate prediction require a meaningful ensemble of model configurations that represent the limitation of observations to constrain arbitrary choices in model formulation such as the values assigned to its multiple, non-linearly related parameters. We present a data directed importance sampling strategy that makes optimal use of distributed computing resources and improves the sampling efficiency over uniform or random sampling strategies by several orders of magnitude. The algorithm is then further developed to take into account uncertainties in our ability to establish a

normalized metric of model-data distance owing to the correlations that exist in space and time among the 15 fields that are used to evaluate model skill. By incorporating estimates of this uncertainty in the prior, further improvements can be attained in the accuracy and efficiency of the stochastic sampling algorithm. The algorithm is then applied to estimating an *a posteriori* probability density for 6 parameters important to clouds and convection of the Community Atmosphere Model version 3.1. The top six performing parameter sets improved model skill by 10% with nearly identical skill scores, but for different reasons related to the wide range of selected parameter values. Efficiently quantifying these uncertainties will provide important insights into the limitations of climate model predictive skill within a time frame practical for climate model development.

#### 1. Introduction

The 2001 Working Group I report from the Intergovernmental Panel on Climate Change (IPCC, 2001) documents a wide disparity among existing models of the climate system in their response to projected increases in atmospheric CO2 concentrations. Predictions of global mean surface air temperature sensitivity to a doubling of atmospheric CO2 concentration (in ~100 years) range from ~2 to 6 degrees (LeTreut and McAvaney, 2000; Cubasch et al., 2001). There are a number of possible reasons why these differences exist. Although each climate model has been tuned to reproduce observational means, each model contains slightly different choices of model parameter values as well as different parameterizations of under-resolved physics (e.g. clouds, radiation, convection). Climate model uncertainties are primarily estimated from model intercomparison projects (e.g. Gates et al. 1999; Joussaume and Taylor 2000; Meehl et al., 2000; also see

that the range of behaviors exhibited by models that participate in the intercomparison projects is representative of a realistic range of probable outcomes (e.g. Meehl et al., 2000). Although there may be some recognition of which models perform better than others, the qualitative approach to evaluating model performance does not lend itself to assigning quantitative likelihoods to model predictions. The 2001 IPCC report, in its assessment of current research needs, calls for "...a much more comprehensive and systematic system of model analysis and diagnosis, and a Monte Carlo approach to model uncertainties associated with parameterizations..." (Section 8.10, McAvaney et al., 2001). The computational expense of typical atmosphere-ocean general circulation models (AOGCMs) is a major barrier to reaching this goal. Two approaches have been taken to address uncertainties arising from climate model parameters. One is based on a reduced complexity climate model (Forest et al., 2000, 2001, 2002) and the other one distributes the computational burden among thousands of under-utilized personal computers (see www.climateprediction.net; Allen, 1999; Stainforth et al., 2005). Data directed importance sampling for climate model parameter uncertainty estimation concerns an improved framework for taking advantage of distributed computing resources toward the goal of identifying multiple, non-linearly related parameter values of a single climate model that reflect observational constraints on climate model uncertainty. This goal is not trivial insofar as a single climate model experiment typically uses a 30-year simulation or 1500 cpu hours to characterize a climate state and one may need to complete millions of experiments to randomly sample all the potentially relevant combinations of 10 or more parameter values.

www.clivar.org/science/mips.htm for a list of 31 ongoing projects). It is often assumed

Predictive uncertainty up to this point has been mainly associated with uncertainty in CO2 emissions and/or natural variability, factors that may be treated in a fairly straightforward manner. A far greater challenge is to represent the uncertainty that arises from arbitrary differences in climate model parameter values when the parameters themselves are non-linearly related (Kheshgi and White, 2001). This fact presents unique challenges to those working to improve climate model predictions. One example of this challenge became apparent within a presentation at the 2001 NCAR Community Climate System Model (CCSM) Workshop in Breckenridge, Colorado. In an effort to improve simulations of arctic climate, changes were made within the infrared radiation scheme to make it more physical. This had the effect of improving the simulation of arctic climate but at the expense of drying out the tropics. This was remedied in part by increasing the amount of water that is allowed to evaporate from hydrometeors (rain drops) within unsaturated downdrafts of convective clouds. In another particularly dramatic example, Williams et al. (2001) document the effect of specific changes made in the process of creating the next version of HadCM2 (Hadley Center Climate Model 2, United Kingdom). The authors noticed that the response of precipitation over the tropical Pacific to a doubling of atmospheric CO2 concentration within HadCM3 was entirely different from the distribution found within HadCM2. The cause of these differences was found to originate from the combined influence of small changes within two parameters affecting mixing within the boundary layer and the critical humidity for cloud formation. Many of these non-linear behaviors within models go unpublished, as the root causes are often hard to identify and there often is not a strong link to any particular science question.

Wiley STM / Editor: Advanced Computational Infrastructures for Parallel and Distributed Adaptive Applications, Chapter 6 / Authors Jackson, Sen, Stoffa, Huerta / filename: ch6.doc However, even these few examples underscore the need for a systematic approach for evaluating climate model performance and a way to navigate through the seemingly endless cycle of 'educated guessing' that now takes place each time a new version of a climate model is released.

There are two useful objectives to an uncertainty analysis that considers how non-ideal parameter value choices affect model predictions of climate. The first is to identify sets of model parameter values that define members of an ensemble that is assured to be representative of the combined uncertainty in the observations and model physics. The second is the ability to identify an optimal set of parameter values that maximizes climate model performance. As of yet, there has been little progress on meeting these objectives outside of what can be gleaned from individual sensitivity experiments and model intercomparison projects. The principal reason for this lack of progress is that most traditional methods for meeting the first objective (e.g. Monte-Carlo or Metropolis/Gibbs' 'importance sampling') require  $10^4$  to  $10^6$  model evaluations (experiments) for problems involving fewer than ten parameters.

Over the past decade, there has been significant progress within the mathematical geophysics community for solving non-linear problems in geophysical inversion using statistical methods to account for the possibility of multiple solutions (interpretations) of geophysical data (for a review, see Barhen et al., 2000). Like climate models, geophysical models are complex, computationally expensive, and involve many potential degrees of freedom. Within the geophysics community, particular emphasis has been

placed on efficiency, although with some measured compromises. Similarly dramatic advances have taken place within the statistics community over the past decade on a class of methods of statistical inference known as Markov Chain Monte-Carlo (MCMC). In particular, greater awareness now exists for how different challenges in robust statistical inference can be addressed with Bayesian inference and sampling rules that obey the properties of a Markov chain. In what follows we document progress being made on both these fronts to advance the feasibility of quantifying climate model uncertainties that stem from multiple, non-linearly related parameters.

Other, potentially useful approaches exist to estimating parameters and uncertainties for complex systems. Examples include Latin-hypercube sampling and kriging interpolation techniques to reduce the number of experiments that may be needed to estimate the multidimensional dependencies (Sacks et al. 1989; Welch et al. 1992; Bowman et al. 1993; Chapman et al. 1994; Santer et al., 2003). Within the climate community, there has been some interest to apply the Ensemble Kalman Filter which uses time trajectories of the climate system in much the same way traditional data assimilation works in numerical weather prediction (e.g. Grell and Devenyi, 2002; Evensen, 2003; Annan et al., 2007). This may provide another computationally feasible approach to the tuning problem, but this approach still needs to prove its viability for the longer-term climate problem. One concern is that many of the effects and feedbacks of model parameter changes take time to express themselves. The parameter choices constrained by short term weather would not be the same or ideally suited for a model meant for predicting climate change (Lea et al., 2000). The point that will be developed below is that estimates of the posterior distribution and optimization of model skill can be

Wiley STM / Editor: Advanced Computational Infrastructures forpage 7Parallel and Distributed Adaptive Applications,page 7Chapter 6 / Authors Jackson, Sen, Stoffa, Huerta / filename: ch6.docperformed through direct sampling, in parallel, with relatively few iterations and without

surface approximations.

# 2. Computing Climate Model Parameter Uncertainties in Parallel

The computation of parametric uncertainties in a climate model will take advantage of two levels of parallelism; the parallelism of the climate model code and the parallelism permitted by the stochastic sampler. In order to appreciate the advantages of the choice of stochastic sampler it will be helpful to first document the computational characteristics of the Community Atmosphere Model version 3.1 (CAM3.1) for which we are currently testing the effects of 6 model parameters important to clouds and convection. CAM3.1 resolves the physics and fluid motions of the atmosphere on a 64 x 128 spectral grid with 26 vertical levels. For parallelism, the code exploits domain decomposition by the 64 latitude bands which place an effective upper limit on number of processors for which the model can be run efficiently. The performance of CAM3.1 may be expressed by the number of simulated years per wall clock day for a given number of processors. This number may be normalized by the number of processors (years per day per processor) to give a measure of the scaling efficiency of the code. Table 1 shows the performance of CAM3.1 on a distributed computing platform available at the Texas Advanced Computing Center. This platform consists of a distribution of Dell PowerEdge 1955 Blade servers each with dual socket/dual core 2.66 GHz Intel 64-Bit Xeon (Woodcrest) processors and a 1333 MHz Front Side Bus and dual channel 533 MHz fully buffered DIMMS. Each server is interconnected by an InfiniBand switch with a nominal bandwidth of 1 Gigabit/s with 6µs latency, the overhead time for sending a packet of

Wiley STM / Editor: Advanced Computational Infrastructures for Parallel and Distributed Adaptive Applications, Chapter 6 / Authors Jackson, Sen, Stoffa, Huerta / filename: ch6.doc information between any two processors. Climate models do not scale particularly well within distributed computing environments because of the frequency at which information needs to be shared among processors. This makes scaling performance numbers more sensitive to latency numbers.

The performance numbers of table 1 provide a reality check on the enormity of the problem to systematically evaluate all possible combinations of parameter values. Without model parallelism, a single 10-year long experiment would take over a week. In order to take advantage of the data-directed importance sampling described below, one needs at least 150 of these experiments to be run sequentially. We therefore depend on the model parallelism in addition to the stochastic sampling algorithm parallelism to obtain scientifically relevant results within a reasonable time frame.

### 3. Stochastic Inversion

Bayesian statistics uses rules of conditional probabilities to infer how a set of parameters may be constrained by available observations given knowledge of a system's physics. The desired result is known as *a posteriori* probability density function (PPD). The PPD is a powerful summary of information about how observational data can inform us about key relationships of a physical system. The key to making this work efficiently is to allow data to be involved in selecting candidate parameter values through a meaningful metric of the distance between observations and model predictions. That is, the improved efficiencies come from the process by which the choices of candidate parameter values depend on past values. This dependency is not great news for application in distributed computing environments as one wants to be completing as many experiments at once as

Wiley STM / Editor: Advanced Computational Infrastructures for Parallel and Distributed Adaptive Applications, Chapter 6 / Authors Jackson, Sen, Stoffa, Huerta / filename: ch6.doc possible. Moreover, most algorithms for choosing candidate parameter values are not terribly efficient, even when directed by data, and whatever efficiency they do achieve is sensitive to characteristics of the shape of the likelihood function, the metric of modeldata discrepancies as a function of model parameters.

The optimal approach to stochastic inversion for data and/or computational demanding problems is a subject of current research. One strategy that provides an adequate blend of efficiency and accuracy is Multiple Very Fast Simulated Annealing (Sen and Stoffa, 1996; Jackson et al. 2004). The rules for selecting samples is similar to a Metropolis/Gibbs sampler insofar as candidate parameter set values are either accepted or rejected (for stepping through parameter space) in proportion to a probability

$$P = \exp\left(\frac{-\Delta E}{T}\right),\tag{1}$$

where  $\Delta E = E(\mathbf{m}_{k+1}) - E(\mathbf{m}_k)$  is the change in the metric of model-data discrepancies, also called the "cost function", for going from a model with parameter set values  $\mathbf{m}_k$  to model with parameter set values  $\mathbf{m}_{k+1}$ . The mathematical form of  $E(\mathbf{m})$  is defined below. The Metropolis/Gibbs sampler is sensitive to the algorithm "temperature" parameter T which controls how freely the stochastic sampler will jump around parameter space. If too high a temperature is selected, then the benefits of data-directed sampling are lost. If too low a temperature is selected, then sampling will not be representative of the range of possible solutions. Multiple Very Fast Simulated annealing avoids the ambiguity of knowing in advance what the ideal temperature is by starting at a relatively high temperature and allowing the stochastic sampler to experience a range of temperatures according to the schedule in which iteration (k) has temperature

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$T_k = T_o \exp(0.9(k-1)^{1/2}).$	(2)

The size of the steps that are taken through parameter space within MVFSA is connected to temperature with larger steps at higher temperatures and smaller steps as T approaches 0. After a relatively few number of iterations, depending primarily on the dimensionality of **m**, the MVFSA algorithm will converge on a solution that tends to favor the global minimum of the cost function. The convergence process should be repeated 10 to 100s of times to accumulate sufficient statistics to estimate the PPD. The advantage of MVFSA for distributed computing is that the convergence attempt chains can be run in parallel with the final estimate of the PPD coming from an accumulation of statistics across chains. Because of its data-directed sampling, MVFSA can be several orders of magnitude more efficient than the Metropolis/Gibbs sampler (Figure 1). So the combination of the sampling efficiency and the fact that one can separate the problem into multiple pieces brings a new class of problems within reach of Bayesian stochastic inversion.

#### 4. Application to Climate Prediction

Within the Bayesian formulation of probability, the likelihood of a given choice in parameters is measured by an exponential of the effects of those parameters on model performance (*i.e.* the cost function) relative to all other parameter choices tested. The use of exponential implies Gaussian errors in both the data and observations. Many potential applications of Bayesian stochastic inversion may not know or may not depend heavily on quantifying these errors. For instance, in some cases it may be sufficient to simply identify the locations of the peaks in the PPD and exhibit the uncertainty as a qualitative Wiley STM / Editor: Advanced Computational Infrastructures forpage 11Parallel and Distributed Adaptive Applications,Chapter 6 / Authors Jackson, Sen, Stoffa, Huerta / filename: ch6.docre-weighting of the PPD given slightly different scaling factors, S, for the uncertainty in

size in the error normalization (data covariance) part of the metric of model performance,

$$PPD(\mathbf{m}) = \frac{\exp(-S \cdot E(\mathbf{m}))}{\int \exp(-S \cdot E(\mathbf{m}))d\mathbf{m}}.$$
(3)

For the climate prediction problem, where there is more interest in quantifying the likelihood of extremes, it is necessary to develop a more formal way to incorporate information about sources of uncertainty. In the following two sections, we discuss why there exists a need for incorporating prior information acknowledging uncertainties in selecting '*S*' into the definition of the metric of model performance and its role in improving the efficiency and accuracy of estimating the PPD.

# 4.1 Definition of the Metric of Model

## Performance

The cost function  $E(\mathbf{m})$  contains an inverse of the data covariance matrix  $\mathbf{C}^{-1}$  which provides a means to normalize the significance of model-data mismatch among Ndifferent fields  $\mathbf{d}_{obs}$  (e.g. surface air temperature, precipitation, etc...) and model predictions  $g(\mathbf{m})$  at M points (note that each field may contain a different number of points M),

$$E(\mathbf{m}) = \sum_{i=1}^{N} \frac{1}{2N} \left[ \left( \mathbf{d}_{obs} - g(\mathbf{m}) \right)^{T} \mathbf{C}^{-1} \left( \mathbf{d}_{obs} - g(\mathbf{m}) \right) \right]_{i}.$$
 (4)

Equation (1) includes vector  $\mathbf{m}$  of model parameter values and T for the matrix transpose. The data covariance matrix includes information about sources of observational or model uncertainty, including information about uncertainty originating from natural (internal) variability, measurement errors, or theory. This form of the mean square error E is the appropriate form for assessing more rigorously the statistical significance of modeled-observational differences when it is known that distributions of model and observational uncertainty are Gaussian. Our focus here will be entirely on sources of uncertainty that arise from natural variability.

If one assumes uncertainties are spatially uncorrelated, the data covariance matrix will contain non-zero elements only along the diagonal. When considering uncertainty originating from spatially uncorrelated natural variability, each of these elements is equal to the variance of the natural variability within the corresponding grid point where model predictions are compared to observations. However data points are correlated in space, season, and among fields. Some points and/or fields have very little associated variance, such as rain over a desert. The cost function can be very sensitive to the choices one makes in accounting for these correlations and/or singularities within the data covariance matrix (Mu et al., 2004). Estimating normalizing factors for complex systems is an area of active research (Gelman et al., 2004, see page 345). Although not satisfactory to a statistician, some have treated this unknown through a re-weighting of the posterior distribution (*i.e.* S within equation 3). The problem is that such a re-weighting does not give the statistical sampling algorithm the opportunity to only sample from the posterior which can lead to in-efficiencies and biases in the results. A more statistically correct procedure would be to introduce a renormalizing factor before sampling. One empirical Bayesian approach is to estimate S in advanced through an ensemble of experiment in

Wiley STM / Editor: Advanced Computational Infrastructures for page 13 Parallel and Distributed Adaptive Applications, Chapter 6 / Authors Jackson, Sen, Stoffa, Huerta / filename: ch6.doc which one imposes uncertainties. For instance, in the climate problem where the uncertainty is from natural variability, one may consider how the cost function would be affected if the climate model (or data) were taken from different segments of a long integration. One may estimate a fixed re-normalizing factor to be  $S = 2/\Delta E$  where  $\Delta E = E_{95} - E_0$  represents the  $2\sigma$  range in cost function values that arise from internal variability. One may then apply the logic that parameter sets that are  $\Delta E$  away from the optimal parameter set will be given a likelihood measure of exp(-2), which is equivalent to the 95% probability measure for a normalized Gaussian distribution.

# 4.2 Incorporating Uncertainties in Error Normalization in the Prior

The re-weighting of samples according to equation (3) give a skewed perspective of the PPD as it tends to have more narrow peaks and fat tails relative to a cost function that had been correctly normalized. This is because correlations among constraints in the data tend to increase the significance of changes in the cost function. Thus stochastic sampling uninformed about the effects of these correlations will tend to sample more frequently the regions that end up being weighted down in equation (3). This represents a sampling inefficiency.

Along the lines suggested by Gelman et al. (2004) it is possible to treat S as one of the uncertain parameters within MVFSA and use principles of Bayesian inference to select

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candidate choices of *S* from a prior Gamma distribution whose mean and variance is determined by a process similar to the choice of *S* in Section 4.1. The choice of a Gamma distribution was mostly for mathematical convenience and given that a Gamma prior is "conditionally conjugate" to our definition of the cost function. It is a mathematical way to express uncertainties in the denominator (i.e. the variance). The Gamma distribution looks alike a skewed Gaussian distribution with no probability for a value of 0, a mean value that corresponds to the choice of S from the previous section, and a tail that conveys uncertainties in defining an appropriate S. In a fully Bayesian approach, one can construct candidate choices of *S* to depend on a corresponding evaluation of  $E(\mathbf{m})$  in order to incorporate uncertainties in the data covariance matrix into the stochastic sampling algorithm (Jackson et al, in prep).

Although this revised method adds a randomly generated number S to the acceptance/rejection criterion (equation 1), there can be significant improvements in the accuracy and efficiency (Figure 1) to estimating the PPD. In fact, samples selected in the case where *S* is included through a prior no longer require weighting for estimating the PPD as these samples are now assumed to be drawn directly from a distribution that is proportional to the actual PPD. The effect of this choice can be dramatic as illustrated in Figure 2 where the PPD derived from including *S* as a prior is a much better match to the target distribution of an idealized example than without it.

#### 5. Results

The MVFSA stochastic sampler has been applied to estimating the PPD of six parameters (Table 2) of the Community Atmosphere Model version 3.1 (CAM3.1) important to clouds and convection as constrained by observations or reanalysis of 15 fields separated into 4 seasons and 6 regions covering the globe (Mu et al., 2004). In addition MVFSA incorporates a prior distribution estimate for *S*, the parameter controlling inadequacies of properly defining the data covariance matrix (Jackson et al, in prep).

Each experiment testing the sensitivity of CAM3.1 to combined changes in select parameters follows an experimental design in which the model is forced by observed sea surface temperatures (SST) and sea ice for an 11-year period (March 1990 through Feb. 2001). The model includes 26 vertical levels and uses an approximately 2.8° latitude by 2.8° longitude (T42) resolution.

Up to this point 518 experiments have been completed over 6 independent VFSA convergence attempt "lines". Each line starts at a randomly chosen point in the multidimensional parameter space. Each model experiment runs in parallel over 64 processors, bringing the total number of processors being occupied at any point in time to 384. The average number of experiments that we anticipate will be required to reach convergence for each line is 150 (Jackson et al, 2004). We therefore estimate that we are about two thirds of the way toward a stationary estimate of the PPD. Wiley STM / Editor: Advanced Computational Infrastructures for Parallel and Distributed Adaptive Applications, Chapter 6 / Authors Jackson, Sen, Stoffa, Huerta / filename: ch6.doc page 16

Of the 518 completed experiments, 332 configurations have cost values the same or better relative to the default model configuration with the optimal experiments in each line averaging a respectable 10% improvement in their cost values. The size of the cost function gives a normalized perspective of the distance between observations and model predictions with the units relating to the size of the effect of internal variability on each component. Large cost values tend to be associated with fields that have very little variability. In this case the field with the largest associated cost value in the default model configuration is the annual mean global mean radiative balance at the top of the atmosphere with a value of 202 cost units. The field with the lowest cost value is precipitation with a value of 24.2 cost units.

We have separately analyzed the six top performing experiments, one for each of the independent lines considered. The fields that improved the most across these six experiments were shortwave radiation reaching the surface (averaging 14% improvement), net radiative balance at the top of the atmosphere (33% improvement), and precipitation (12% improvement). However, the performance gains or losses for the other fields were not consistent. The similar cost values achieved for all six optimal model configurations is achieved through different compromises in model skill for predicting particular fields.

The marginal PPD for each of the six model parameters along with the position of the default model and the optimal values chosen by the six lines is shown in Figure 3. The PPD is generated only from the 332 configurations that have the same or better cost than

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the default configuration. The range of parameter values that improved model

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performance is quite broad for all parameters except for the critical relative humidity for low cloud formation. Also of interest is the desired result that the six optimal parameter sets are representative of the uncertainty as quantified by the PPD. Capturing climate model parametric uncertainties within a limited number of candidate model configurations is the key step in quantifying observational constraints on these important degrees of freedom for model development. For instance, one may use these different parameter sets to test the impacts of these uncertainties on the model's sensitivity to CO2 forcing. Although we are still a third of the away from completing the number of necessary experiments to draw a firm conclusion, the implication of the wide ranges apparent in Figure 3 is that it may be very difficult to use available observations to constrain sufficiently some of the choices that need to be made in assigning values to parameters that are involved in clouds and convection which are processes thought to be key sources of climate prediction uncertainty.

### 6. Summary

The increase in availability in distributed computing provides an opportunity for the climate sciences to address more quantitatively the sources and impacts of uncertainties in climate model development on climate predictions. This is achieved through a selection of alternate climate model configurations that reflect the scientific values for how these models are constrained by observations (i.e. the definition of the cost function). One of the barriers to achieving this goal is the substantial computational Chapter 6 / Authors Jackson, Sen, Stoffa, Huerta / filename: ch6.doc

dependent. For these cases, one needs to draw inferences about the relative likelihood of different possible choices from a random sampling of candidate parameter combinations that do not bias the end result. Data directed importance sampling achieves improved efficiency from sampling more often, and in proportion to the final PPD, those regions of parameter space that contribute effectively to the PPD. There exist many types of stochastic samplers that make use of data-direction. However, many of these approaches depend on the sequential integration of experiments which make it difficult to fully exploit available computational resources. Moreover, the efficiency of most methods depends on knowledge about the characteristics of the problem which may be difficult to gage without significant experimentation. We present Multiple Very Fast Simulated Annealing (MVFSA) as an alternative which is less sensitive to problem characteristics and produces helpful estimates of the PPD.

expense of climate models where the ideal choice of multiple parameter values is inter-

We also show that additional improvements in accuracy and efficiency of the MVFSA algorithm can be incorporated into data-directed importance samplers when prior information is incorporated about the size of the effects of sources of uncertainty on the cost function through a parameter '*S*' which is conceptually correcting for errors in defining a data covariance matrix that appropriately accounts for correlations that may exist among the many data constraints.

The results of estimating a PPD for 6 parameters of the CAM3.1 climate model reinforce the notion that there exist many possible model configurations that can do an

Wiley STM / Editor: Advanced Computational Infrastructures forpage 19Parallel and Distributed Adaptive Applications,page 19Chapter 6 / Authors Jackson, Sen, Stoffa, Huerta / filename: ch6.docequally adequate job in reproducing a multi-field average skill score. More sampling willbe required to establish with greater confidence the relative likelihood of the solutionsthat have been identified so far. The main point of this exercise is to illustrate thepracticality of data-directed importance sampling and uncertainty characterization ofparameters within a non-idealized climate model.

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Wiley STM / Editor: Advanced Computational Infrastructures for Parallel and Distributed Adaptive Applications, Chapter 6 / Authors Jackson, Sen, Stoffa, Huerta / filename: ch6.docpage 25Table 1. Performance of CAM3.1 over a cluster of Dell PowerEdge 1955 Blade serversParallel and Structures for Parallel and Distributed Adaptive Applications, Chapter 6 / Authors Jackson, Sen, Stoffa, Huerta / filename: ch6.docParallel and Distributed Adaptive Applications, Parallel Adaptive Applications, Chapter 6 / Authors Jackson, Sen, Stoffa, Huerta / filename: ch6.docParallel Adaptive Applications, Parallel Adaptive Applic					.5		
# of processors	1	2	4	8	16	32	(
Simulated years/wall clock day	0.92	1.70	2.91	5.56	10.26	17.91	2
Simulated years/wall clock day	.92	.883	.729	.696	.641	.560	
per							

processor

#### Table 2. Names and descriptions of parameters important to clouds and convection

#### in CAM3.1

Parameter	description
RHMINL	critical relative humidity for low cloud formation
RHMINH	critical relative humidity for high cloud formation
ALFA	initial cloud downdraft mass flux
TAU	rate at which convective clouds consume available potential energy
ke	environmental air to cloud entrainment rate coefficient
c0	deep convection precipitation production efficiency parameter



Figure 1. Convergence fraction as a function of experiment number for MVFSA not incorporating S into the stochastic sampling (red line), MVFSA with incorporating S into the stochastic sampling (black line), and the Metropolis/Gibbs sampler (green line). Convergence fraction is given by the rms difference among the distributions for 6 climate model parameters as a function of experiment number and the final distribution. The climate model is described in Jackson et al. 2004.



Figure 2. Idealized example using different sampling schemes. Sampling efficiency is improved when information about 'S' is included within the prior. Target distribution (gray bars) was generating using Gibbs' sampling using a prior for 'S'. Gibbs' sampling without a prior for 'S' is given by the dashed blue line. MVFSA sampling using a prior for 'S' is given by the solid red line and without using a prior for 'S' is given by the dashed red line.



Figure 3. PPD for 6 parameters of CAM3.1 important to clouds and convection (see Table 2). The histograms are derived from the 332 experiments whose cost values were the same or showed an improvement of over the default model configuration. The parameter values of the default model are given by an asterisk (\*). The values of the top performing six parameter sets are labeled by the particular line number that produced them.